Shock Waves in Materials with Dzugutov Potential Interactions

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(Dated: June 1, 2005)

The influence of shock waves on the bcc ground state, the metastable \( \sigma \)-phase, and quasicrystal structures of the Dzugutov potential [Phys. Rev. A 46, R2984 (1992)] has been studied by molecular dynamics. In general, a phase transition is observed to the well-known high-pressure fcc- or hcp-phases. The details of the phase transition and the perfection of the created phases depend on the orientation of the shock wave propagation direction with respect to the symmetry axes. The results are in good qualitative agreement with recent simulations with EAM-potentials designed specifically for iron. For the quasicrystal we observed flips, a new plasticity mode predicted for these structures. Furthermore we will report the results for an amorphous structure supplied with the same potential.

No crystallization takes place in this case, indicating that it is easier to shift atomic layers collectively than to order the atoms one by one.

PACS numbers: 62.50.-p, 61.14.Br, 62.70.Ns

Keywords: quasicrystals, shock waves, molecular dynamics simulations

I. INTRODUCTION

Shock wave experiments and simulations are useful tools to expose a solid to strong uniaxial stress and to study plasticity induced by defects or phase transitions without prior assumptions about the possible mechanisms. The action of shock waves has been explored in monatomic crystals to some depth\(^1,2\), and a first understanding of the basic processes has emerged\(^3\). The generation of partial dislocations and stacking fault type defects in fcc crystals could be clarified\(^4\). Results for the plasticity of other structures, like bcc-iron for example, are also available now\(^5\).

The purpose of the present study is to find out whether monatomic quasicrystals behave different than crystalline materials if they are penetrated by shock waves. Most naturally occurring quasicrystals are ternary alloys. Stable binary quasicrystals have been discovered only very recently\(^2\). Shock waves in binary quasicrystals have been studied, and it was found that the results for quasicrystals and crystals depend primarily on the atomic interaction and not on the structure\(^6\).

From a fundamental point of view it is more interesting, however, to study models as simple as possible, i.e. monatomic quasicrystals. But the number of such models is rather limited if generic interactions are favored. The crucial point is the packing density. There is the unit sphere packing model of Henle\(^8\) with a density of 0.6288, still worse than the random close packing at 0.6336. Treated as a quasicrystal with Lenard-Jones interactions, the structure is metastable only up to 10% of the melting temperature of the ground-state fcc crystal\(^9,10\). It is the only promising monatomic icosahedral quasicrystal model known to us. Henley's twelvefold site model\(^9\) has a much lower packing density and is even less stable. Other models are layered quasicrystals which are periodic in one direction. The decagonal model of Cockayne and Mihalkovic\(^11\) has a packing density of 0.6953, higher than the icosahedral model and larger even than bcc. But it also transforms into fcc upon heating if the atoms interact via Lenard-Jones potentials. Finally there is a dodecagonal quasicrystal model with Dzugutov potential interactions. Its phase diagram has been studied in detail\(^12,13\). Although Dzugutov\(^14\) has obtained a quasicrystal by cooling a melt, it is not a ground state for this interaction at zero temperature. Another crystal structure, namely the \( \sigma \)-phase, which may be regarded as a low-order quasicrystal approximant, is more stable than the quasicrystal. But even more stable and the true ground state at zero temperature is a bcc crystal. The stable structures at high pressure and low temperature are even close-packed fcc- or hcp-phases. Upon heating at low pressure bcc-, the \( \sigma \)-phase and the quasicrystal phases are stable up to rather similar melting temperatures. This is the reason why shock-wave simulations have been carried out with these structure models and the Dzugutov potential.

The work is being described in two papers: Here we present the results of shock wave simulations in the different structures stable with Dzugutov interactions. In a second article\(^15\) (called Paper II in the following) we concentrate on the phenomenon of solitary waves observed especially in the bcc structure shocked along the threefold axis and discuss in detail the hexagonal \( \omega \)-phase\(^16\), a typical product of an bcc lattice instability. The present paper is organized as follows: We first describe the simulation setup and the structure models. The next sections contain the results for each of the models and for the different orientations, followed by a short account of the soliton phenomenon. A thorough discussion of the latter will be given in the second paper. We close with a discussion of the results.
II. GENERATION OF THE SHOCK WAVES AND SIMULATION SETUP

A. The Structures

Shock waves have been generated in three-dimensional dodecagonal quasicrystals, in the Frank-Kasper-type $\sigma$-phase and in bcc crystals. The bcc structure may be regarded as a tetrahedrally close-packed phase (tcp) and therefore has some similarity to the Frank-Kasper phases. From this point of view bcc contains disclinations where six tetrahedra meet along a common edge and anti-disclinations where four tetrahedra meet, whereas ordinary Frank-Kasper phases contain disclinations only. The $\sigma$-phase is such an ordinary Frank-Kasper phase with squares and triangles as basic motives. The $\sigma$-phase and other related phases together with dodecagonal quasicrystals have been described in detail by Roth[12]. Here we will recollect only the most important aspects of the structure.

The unit cell of the $\sigma$-phase can be subdivided into building blocks which look like two regular triangles and two squares if projected onto the basis plane perpendicular to the four-fold direction (Fig. 1). The building blocks will be called tiles in the following and we will simply speak of squares and triangles. Two squares and three triangles meet at each vertex in such a way that the squares have no common edge. The arrangement of the atoms can be read off from Fig. 1: The vertices of the squares and triangles are decorated with atoms at $z = 0$ and $z = 1/2$ (dotted circles). These are the basic $A$ layers. The edge centers of the squares are alternatively decorated at $z = 1/4$ and $z = 3/4$ (filled and empty circles). The interior of the squares contains four additional atoms. Atoms nearest to each other in projection are placed in different layers. The atoms at the edge centers of the triangles are all either at $z = 1/4$ or at $z = 3/4$, the interior atom is again in the layer not occupied by the edge atoms. The atoms at $z = 1/4$ and $z = 3/4$ form the $B_-$ and $B_+$ layers, respectively, locally equivalent up to translations and rotations. The atoms at the vertices of the tiles are 14-fold coordinated, while the atom in the center of the triangles is 15-fold coordinated. The remaining atoms on the edges and in the interior of the square are 12-fold coordinated non-regular icosahedra. Since all coordination shells have a triangular surface, all atoms are tetraddextrally close packed.

Other combinations of squares and triangles are also possible. There are three additional phases in which all vertices are of the same type[19]. They are presented in Fig. 1. These phases are less stable than the $\sigma$-phase, so they will not be considered further in this paper. If more than one vertex type is allowed the number of possible phases grows very rapidly, even for crystalline structures[20].

The quasicrystal is built of the same square and triangle tiles. We have studied random tilings only in this paper although it is possible to construct perfect quasicrystals with the help of matching rules or by inflation. In the quasicrystal model the tiles of the primary layer are arranged in such a way that the structure has dodecagonal symmetry on average. The $B_-$ and $B_+$ layers have hexagonal symmetry only. They are mapped onto one another by the twelve-fold symmetry. It is possible to introduce additional tiles, for example the hexagons (see Fig. 2), and to construct more general quasicrystalline structures, but they will not be considered here since these configurations are not as stable as the pure square-triangle tiling.

Additional tiles are found in crystalline samples already (see Fig. 2). Especially rhombi may occur as localized defects or represent grain boundaries. The rhombi are not stable if they occur in pairs or larger aggregates. The two hexagons have not been observed in crystals. They may be viewed as transition states which can split into the other tiles.

Figure 3 represents a special approximant of a quasicrystal which has been chosen such that most of the tiles and vertex configurations are present.

B. Orientation of the Samples

For the simulation of shock waves it is necessary to apply periodic boundary conditions. Otherwise the pressure from the shock wave leads to rapid transverse disintegration. The direction of the shock wave has to be parallel to one of the boundary axes, for example the $x$-axes. This limits the possible (quasi-)crystalline directions along which the shock wave can travel in the simulations. The quasicrystal, especially, has to be replaced by an orthorhombic approximant. Shock waves have been studied in the bcc-phase along the four-, three-, and two-fold axes where they are straightforward to im-

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**Fig. 1:** Possible vertex configurations in square-triangle tcp-phases. From left to right: $A$-phase, $Z$-phase, $H$-phase, and $\sigma$-phase.

**Fig. 2:** Primary and additional tiles observed in the square-triangle tcp-phases. From left to right: square, triangle, rhombus, three-fold and two-fold symmetric hexagon.
FIG. 3: Part of a dodecagonal quasicrystal. The atoms in the basic A layers z = 0 and z = 1/2 are dotted. The black atoms are in the B layer at z = 1/4, the white atoms are in the B layer at z = 3/4. The edge length is usually of the order of 2a, the nearest neighbor distance, but depends on the interaction between the atoms.

plement. Shock waves in the square-triangle quasicrystal have been studied along the periodic axis and in the quasiperiodic plane. Due to the high twelve-fold symmetry (space-group 12/z/mnm) the quasicrystal is expected to be elastically isotropic in the plane, and the approximant should not deviate too much from isotropy. Shock waves along different in-plane directions should therefore give similar results. The σ-phase has space-group symmetry 4/mmm, which means that for an ordinary, nearly cubic unit cell with 60 atoms the coordinate axes are parallel to the four-fold axis and to glide planes n, and the diagonals are parallel to mirror planes m. A diagonal tetragonal unit cell with 30 atoms is also possible with the four-fold axis and the m-planes parallel to the coordinate axes. The aspect ratio of these two unit cell lengths in the plane and along the z-direction is such that it is possible to construct "diagonal" cubic boxes with only minor distortion of the structure and to rotate them by 45 degrees. In summary we have studied shock waves in the σ-phase along the four-fold axis, along the n- and m-directions, and along orientations at 45 degree between the four-fold direction and n and m, respectively. The directions will be denoted by 0, 90, 90, 45 and m45. The corresponding Miller indices are [100], [001], [101], [011], and [√11].

FIG. 4: Left: the Dzugutov potential in the parameterization applied in this work. Right: semi-quantitative phase diagram of the Dzugutov potential. The stress-temperature curves for shocked states are presented for materials initially amorphous (Sec. III C5) and bcc shocked along the two- and four-fold axes (Sec. III). The curves for other initial structures and directions are similar to bcc.

C. The Dzugutov Potential and Phase Diagram

Reduced units are used throughout the paper. Lengths are given in a, and energies in e. All other units are converted into a, e and the mass m. Thus we have \( t_0 = a \sqrt{m/e}, v_0 = \sqrt{r/m}, \) and \( P_0 = e/a^3. \)

Dzugutov has invented his potential\textsuperscript{17} to study the glass transition of monatomic liquids. It turned out that the potential has a number of interesting properties, especially that it stabilizes monatomic dodecagonal quasicrystals. It is similar to the Lennard-Jones potential from the core down to the minimum at \( r = 1.061a \) and \( V = -1e, a \) being the interatomic distance (See Fig. 4, left). The minimum is followed by a maximum at \( r = 1.5282a \) and \( V = 0.7906e, \) designed to disfavor square arrangements of nearest neighbor atoms prominent in close-packed crystal structures at ambient pressure. The potential has a built-in cutoff radius of \( r_c = 1.805a. \) If the density of the structure is increased, the interatomic distances shift, and the close packed structures becomes more favorable than bcc and the σ-phase.

The phase diagram of the Dzugutov potential has been determined by means of molecular dynamics simulations and thermodynamic perturbation theory\textsuperscript{18} and improved recently by direct free energy calculations at low temperatures\textsuperscript{18} (See Fig. 4, right). It turns out that the bcc-phase is the ground-state only in a very small triangular pocket between \( kT = 0, P = 0, kT = 0.4e, P = 0, \) and \( kT = 0, P = 5.5P_0, \) but is metastable in the whole range of stability of the σ- and quasicrystal phases. Close-packed phases with different stacking sequences are largely degenerate due to the short range nature of the
potential which ranges only up to the third neighbor shell. These phases are stable above about $P = 6P_0$. The phase boundary moves slowly to higher pressures with increasing temperature and reaches $P = 10P_0$ at $kT = 1\varepsilon$ ($kT = 1.02\varepsilon$ is the melting temperature of the $\sigma$- and the bcc-phase at $P = 0$). The $\sigma$-phase seems to be the stable phase below $P = 6P_0$ and above the domain of the bcc-phase. Care must be taken here, however, since with increasing temperature other tcp-phases and especially the quasicrystal phase may become more stable than the $\sigma$-phase due to the additional entropy caused by the freedom to (re-)arrange the tiles. The location in the phase diagram where the quasicrystal phase has been discovered is indeed included in the stability domain of the $\sigma$-phase.¹⁴

### D. Sample Size and Preparation

All simulations have been carried out with the IMD which means ITAP Molecular Dynamics simulation package.²⁴ The sizes of the samples depend on the structures and orientations. Therefore, they will not be listed in detail. For most of the simulations the sample size was about $20 \times 20 \times 100\alpha_0$. The samples contained about 40,000 atoms. To study the influence of the size of the samples and the propagation time of the shock wave on the results longer (200, 300 and 600a long with up to 250,000 atoms) and thicker samples (40 $\times$ 40 $\times$ 300$\alpha_0$ with 500,000 atoms) have also been analyzed. The principal results are found to be independent of the sample sizes. There were no differences in the details, but there were no differences for example in the shock wave propagation velocities or in the phase transitions.

Equilibrations were performed with the NVT Nose-Hoover and NPT Andersen ensemble. At low temperature and pressure the differences between NVT and NPT equilibration are marginal. Before the simulation starts the samples are equilibrated for a time interval of $\Delta t = 10\tau_0$ at a temperature of $kT = 0.001\varepsilon$ and a pressure of $P = 0.01P_0$. If the simulations are carried out at elevated temperatures, the samples are equilibrated again at the desired temperature. If necessary, the samples are quenched to $kT = 0.0$ after simulation to simplify the analysis of the results.

For the shock simulations an NVE ensemble was used. There are a number of well established methods to generate shock waves in simulations.²⁵ In the present work we have applied the momentum mirror method: As soon as the atoms reach the upper end of the sample, their velocities are inverted. Thus the atoms behave as if a second sample is colliding with the simulated one. Tests have shown that the results for the mirror method are equivalent to the simulation with the collision method. Consequently the boundary conditions are periodic only in transverse direction whereas open boundaries exist at the end of the sample opposite to the mirror.

### E. Analysis Tools for the Shocked Structures

If the shocked state is monocrystalline as for bcc shocked along the four-fold direction at low piston velocities then the analysis can be carried out directly by visual inspection of the structures. The stacking sequence can be derived from a projection of the atoms perpendicular to the distinguished threefold axis: A zigzag pattern determines hcp, a diagonal sequence fcc. In general we find a mixture of both.

Usually the shocked crystals are very defective, the lattice rows and planes are warped and rotated, twins or several crystallites may exist. A direct distinction between fcc or hcp or more complicated stackings is no longer possible. The radial distribution function (RDF) tells us only that a close-packed phase has been generated (Fig. 5).

But if the angular distribution function (ADF) is computed for nearest neighbor atoms only, then it is possible to distinguish fcc and hcp (Fig. 6) since hcp permits an additional maximum between 140 and 160 degree (the angle between the apex atoms and a base atom of two face-connected tetrahedra). In most cases a mixture of fcc, hcp and other stacking sequences is found.

We have tried to quantify the fraction of fcc and hcp using the common neighbor analysis.²²,²³ The first difference between fcc and hcp occurs for the 1421 and 1422 diagrams. In fcc crystals there are no 1422 diagrams whereas the fraction of 1421 and 1422 diagrams should be equal for hcp. There is a problem, however: In amorphous structures the 1422 are twice as frequent as the 1421. Thus it is not possible to distinguish fcc and hcp quantitatively by the 1421 and 1422 diagrams if substantial disorder is present. The inclusion of other diagrams into the analysis like 1555, 1554, 1433 for icosahedral order or the most frequent second neighbor diagrams 2333, 2211 and 2100 did not help to resolve the ambiguities.

![Typical radial distribution function](image)

**FIG. 5:** Typical radial distribution function. The spikes indicate the neighbor shells for ideal fcc (x) and hcp (□) crystals. Obviously, these cases cannot be distinguished in the simulation result.
III. RESULTS

The stress-temperature behavior of the shocked material is included in the equilibrium phase diagram (Fig. 4). The curves are rather similar for all initial structures as far as a unique temperature can be defined. This is not the case within the transition region from unshocked to shocked where the initial structure is destroyed in several steps and the final structure has to be formed. For details see the Sec. III C. Thus we do not find a thin shock front to which we could apply the standard jump conditions. The stresses and temperatures have been determined directly from the simulation results of the shocked state. The stress-temperature curves are always very steep and do not cross the melting line up to very high pressures ($P > 180P_0$).

In the following sections we will present the results of the shock wave simulations in detail. We will start with the elastic properties of the materials since they form the limiting case of very weak shock waves where the strength of the material prohibits the creation of defects. The next step is the discussion of the relation between the piston velocity $u_p$ and the speed of the shock wave $u_s$ represented in a Hugoniot diagram. In the uniaxial method setup the shock velocity is obtained from the velocity of the sample $u_p$ and the shock propagation velocity $v$ observed in the laboratory reference frame by $u_s = v + (-u_p)$. The Hugoniot diagram permits a classification and characterization of different shock wave regimes. Following is a presentation of the phase transformation results grouped together with respect to similar phenomena.

| TABLE I: Elastic properties for the bcc-phase. The first column gives the Miller indices, the second the uniaxial elastic modulus and the third the velocity of the quasilongitudinal wave. The bcc crystals are obviously anisotropic. |
|-----|-----------------|-------|
| direction | $F[Fb/m]$ | $c/[\nu]$ |
| [100] | 287.0 | 16.6 |
| [110] | 387.0 | 19.3 |
| [112] | 389.4 | 19.4 |
| [111] | 424.8 | 20.2 |

| TABLE II: Elastic properties of the tcp-phases. The first column gives the Miller indices, the second and fourth the uniaxial elastic modulus and the third and fifth the velocity of the quasilongitudinal wave for quasicrystals and the $\sigma$-phase, respectively. The first three rows contain the results for the perfect samples, the last two rows list the results for samples which have been distorted to permit periodic boundary conditions parallel to the 45 degree direction. A comparison of the second and third row and the fourth and fifth row respectively, shows that the quasicrystal is isotropic within the error margins whereas the $\sigma$-phase possesses a moderate anisotropy of the order of 6%. |
|-----|-----------------|-----------------|-------|-------|
| direction | $F[Fb/m]$ | $c/[\nu]$ | $F[Fb/m]$ | $c/[\nu]$ |
| quasicrystal | | | | |
| [100] | 298.4 | 16.8 | 299.2 | 16.8 |
| [010] | 179.2 | 13.0 | 180.4 | 13.1 |
| [011] | 177.0 | 13.0 | 203.0 | 13.9 |
| $[\sqrt{5}11]$ | 216.8 | 14.3 | 248.0 | 15.4 |
| $[\sqrt{3}11]$ | 200.6 | 13.8 | 208.2 | 14.0 |

A. Elastic Properties and Sound Velocities

Dodecagonal quasicrystals behave elastically isotropic with respect to the quasicrystalline plane, but not with respect to the periodic axis, similar to hexagonal crystals. The $\sigma$-phase is anisotropic in the square-triangle-plane since it has only tetragonal symmetry. The bcc crystals have cubic symmetry. The elastic constants determined by quasistatic uniaxial deformations are presented in Tabs. I and II. If the piston wave velocity $u_p$ goes to zero, the shock wave velocity tends towards the velocity of an elastic sound wave.

It is important to note that the highest velocities of sound occur along directions perpendicular to the thinnest crystal planes, or equivalently, parallel to the densest atomic rows. This are the directions where the solitary waves (See Paper II) are most prominent.

B. The Hugoniot Relation $u_s$ vs. $u_p$ and Wave Profiles

In the case of shock waves in two-atomic Laves-crystals and quasicrystals three regimes of different behavior of

FIG. 6: Typical angular distribution function. The spikes denote the angles in ideal fcc (x), hcp (□), and bcc (*) respectively. The simulation result does not fit to the bcc maxima, but to fcc or hcp. A distinction between the latter is possible since the maximum between 140 and 160 degrees is only present in hcp. The conclusion is that the sample under consideration is preferably hcp stacked. Cases without a maximum between 140 and 160 degrees have also been observed.
the shocked materials have been observed. The same is true here, although at a first glance the Hugoniot diagram (Fig. 7) looks different: There seem to be only two ranges, separated at about $u_p = 0.25 c_z$, if $c_z$ is the uniaxial velocity of sound of structure $x$.

The reason is that the elastic first range is very small since the transition from bcc and $\sigma$-phase to close-packed takes place at about $P = 5.5 - 6P_0$, and this pressure is reached at $0.03 - 0.05 c_z$. Furthermore no retardation effect is observed. The elastic wave velocity is difficult to determine since no sharp wave fronts exist. Therefore it is not included in the diagram.

In the range between $u_p = 0.05$ and about $0.2 - 0.25 c_z$, we observe steady and unsteady wave fronts, depending on the orientation of the samples and the character of the phase transition. In this range the shock speed of the uniaxial compression wave is more or less constant whereas the velocity of the slower transformation wave grows rapidly (Figs. 7 and 8). It is remarkable that the two wave fronts taken separately are steady although relaxation and healing of defects occurs for the second. The wave profile as a whole is not steady since the different wave fronts have different velocities.

Above $u_p = 0.2 - 0.25 c_z$ the velocities of both waves approach each other. This part will be called the overdriven range. If the transition is sharp, as in the case of bcc shocked along the four-fold direction, a distinction between both waves no longer exists. In the other cases, especially for bcc shocked in three-fold or two-fold direction two “transformation” wave fronts are plotted: A first one which indicates that the initial phase starts to be destroyed and a high-defect phase is formed, and a second one which indicates the transition to a low-defect close-packed phase. The situation plotted in Fig 8 is typical for short samples. If $u_p = 0.3 c_z$, for example, both transformation fronts have reached the same velocity after a distance of about $70 a$ and the whole wave profile has become steady. If $u_p = 0.5 c_z$ the distance has fallen to $30 a$.

Figure 9 displays some representative hydrostatic pressure wave profiles from all three ranges. In the upper part of the figure it is found that the pressure rises continuously in the elastically deformed part and that this part widens as time goes on. The plastic front on the other hand rises sharply and reaches a steady state. In the lower part of the figure a comparison is given between the wave profiles in the overdriven range in the four-fold direction where a direct transition occurs and the two- and three-fold directions where the bcc structure is first destroyed and a close-packed phase is formed subsequently. This double structure corresponds to the starting and ending of the phase transition as indicated in Figs. 7 and 8.

In conclusion, in the monatomic system a clear distinction exists between an underdriven elastic-plastic regime and an overdriven phase transformation regime for all cases studied, in contrast to the smooth transition which has been observed in the simulations of diatomic materials.

In some cases, especially for shock waves along the three-fold axis in bcc, additional phenomena are observed which will be discussed in detail in Paper II. In the elastic-plastic range a metastable phase is formed which is related to solitary waves observed in the overdriven range. These effects lead to additional wave fronts and wave velocities $u$ and may complicate the analysis of the results. For simplicity, in Fig 8 the wave crests related to the metastable phase and the solitary wave trains are omitted.
FIG. 9: Wave profiles of hydrostatic pressure in the elastic, elastic-plastic and overdriven range. The first three plots are for the four-fold direction, the lower right plot is for a two-fold direction. The profiles in the elastic and the elastic-plastic regime (upper part) look similar for all shock wave directions and initial phases. The arrows in the lower left part indicate the additional wave observed for example for bcc shocked along a the two-fold direction.

C. Description of the Structural Results

Since a lot of structures and orientations have been studied to get a general overview of the possible mechanisms, it is not possible to deal with all the cases in detail and to describe the results in dependence of the piston velocity $u_p$. Instead we will concentrate on a few representative cases, describe them in detail, – especially the dependence on $u_p$ – and add remarks about other structures and orientations where appropriate. We will concentrate on the elastic-plastic range, since in the elastic range no defects are created and in the overdriven range the energy stored in the structure is so high that no low-defect crystals are created during simulation.

1. The Four-Fold Direction

The phase transition from bcc to close-packed phases for shock waves along the four-fold direction is very special. It is the only case where a perfect crystal is found after the transition and an atomically flat interface between bcc and fcc or hcp is observed. Consequently the pressure profile is steady and shows a sharp jump at the interface between bcc and the close-packed phase.

As an example we present the results for $u_p/c_4 = 0.24$ in middle range. Fig. 10 shows the flat interface. The orientation of the close-packed layers is such that a three-fold axis is generated parallel to the shock direction. A two-fold axis is parallel to the face diagonal (Fig. 11, left). This orientation is none of the well-known martensitic bcc-fcc orientation relationships. The stacking sequence of the layers is more or less random but sometimes rather pure fcc or hcp sequences occur. In the right part of Fig. 11 two twins are shown representing a low-energy type of defect. Due to the periodic boundary conditions there have to be two interfaces: one at $y = 8a$ and one at $y = 18a$. If the shock wave proceeds, the twins vanish (Fig.11, right). The twin boundaries end at a dislocation line. We have found that the newly generated close-packed phase may change several times between twined and monocristalline.

The transformed phase remains no longer monocrystalline when the piston velocity enters the overdriven
region. Several crystallites are created, and at about $u_p = 0.5 c_4$ the defect density has grown so large that the sample cannot be distinguished from a disordered or amorphous structure.

2. Other Directions and Structures

Shock waves along the two- and three-fold direction in bcc, in the $\sigma$-phase and the quasicrystal along any direction never lead to a direct transition to the close-packed phase. Although the statistics and the details may differ, the overall pattern of the phase transitions is similar. Therefore we will discuss these cases summarily.

At low shock wave intensity the general picture is the following: The initial structure is heavily distorted or destroyed by the arriving shock front and at the same time structure transformation into the close-packed phase starts.

Two cases can often be distinguished but are usually mixed up: transverse shifts which appear as a bending of the atomic layers (Fig. 12), and more complicated deformations where atomic layers are rotated around an axis parallel to the shock direction in addition to the shifts (Fig. 13). It is remarkable that there are only kinks in the atomic chains parallel to the shock wave direction, but no disruption. Few point-like defects occur at low shock wave intensities. The whole motion of the atoms seems to be well correlated.

The final state of material is a close-packed phase with clearly defined layers perpendicular to the shock direc-
tion, but with several crystallites in the plane. Compared to the bcc case shocked along the four-fold direction, the close-packed crystal has no preferred orientation with respect to the coordinate axes, and it contains many defects and extended disorder. The details of the phase transformation differ for the different structures and orientations. Although the details might be interesting for the study of possible plasticity modes we have collected only the most important cases in Table III.

At the end of the sample, close to the mirror, an almost perfect close-packed crystal is generated (Fig. 12 and 13). This part is clearly induced by the mirror which forces a layering parallel to the mirror. It is not present if the collision method is used. Thus it can be regarded as an artefact. The close-packed phase itself, however, is not a consequence of the simulation method. First of all, the close-packed phase is also created in simulations with the collision method, and second, the close-packed phase is also present in the other parts of the sample as discussed before, but polycrystalline with random orientations of the crystallites and with defects.

The effect of higher piston velocity \( u_p \) is similar to the case of shock waves along the four-fold direction of bcc: the close-packed phase become polycrystalline, more and more defects are created and if \( u_p \) reaches around 0.37 to 0.5c, the structure can no longer be distinguished from an amorphous material.

3. Flipped Configurations in the TCP-Phases

A phenomenon which is called "phason flip" in quasicrystals occurs in the tcp structures shocked along a direction which lies in the basic layer. For simplicity the phason flips can be regarded as tile rearrangements and replacements which are possible in many non-trivial tilings.

Figure 14 shows an example of new rhombi and rearranged tiles in the \( \sigma \)-phase shocked in \( \text{m}90^\circ \)-orientation. The orientations of the tiles are always the same, others are not possible for geometric reasons. In samples shocked in the \( \text{m}90^\circ \)-orientation the rhombi are oriented with their long diagonal parallel to the coordinate axes. In the quasicrystal both orientations are observed. The three-fold symmetric hexagon has also been seen in some occasions, but the two-fold symmetric hexagon never shows up, because it is very unstable. The atomic rearrangements of a flip have been described in detail by Roth\textsuperscript{15}. All the atoms along a row perpendicular to the shock direction change from a one-dimensional configuration of atoms in the basic layer represented by a dotted ring in Fig. 1–3 to a staggered configuration represented by an open and nearby close circle, or vice versa. The tiles themselves are abstract objects which have no physical meaning. Therefore it is not surprising that flips from one-dimensional to the staggered configuration are observed which lead to non-tilable regions.

4. Special Phenomena for Shock Waves along the Three-Fold Direction of BCC

If shock waves are studied in bcc along the three-fold direction an intermediate phase and wave phenomena are observed which are denoted "solitary waves" since they show up as singular, roughly Gaussian shaped dispersionless maxima. We think that this name is appropriate although the solitary waves decay slowly. But since we have not demonstrated the collision property we will not call the peaks solitons. The intermediate phase has been identified as the hexagonal two-layer \( \omega \)-phase\textsuperscript{16}. It is the crystal structure of \( \text{AlB}_2 \) and \( \omega \)-CrTi, and occurs in the phase diagram of the elements Ti, Zr and Hf. The \( \omega \)-phase is also well known as a consequence of phonon softening along the three-fold direction in bcc. The \( \omega \)-phase and the solitary waves are closely related and will be presented in detail in Paper II.

5. Results for an Amorphous Structure

Shock waves have been studied in an amorphous structure produced by cooling a molten bcc crystal. Since there is no liquid phase for the Dzugutov potential at ambient pressures\textsuperscript{12}, we had to prepare the liquid by heating at constant volume, cool it down to \( kT = 0 \), and expand it to \( P = 0 \).

The amorphous structure generated from the liquid
has a RDF which differs from an ordinary monoatomic amorphous structure generated with Lennard-Jones potentials for example. The difference is caused by the outer maximum of the Dzugutov potential: The RDF shows the well-known behavior of a super-cooled liquid with a first maximum for nearest neighbors and a double maximum for next-nearest neighbors, but the first of the two next-nearest neighbor peaks is extremely sharp if compared with what is usually observed. The third maximum seems to be enhanced also. See figure 16 where the curve for \( u_p = 1.00 \) is more or less identical with the unshocked state. The stress-temperature curves for the shocked state has been included in the equilibrium phase diagram (Fig. 4). The curves are somewhat lower than those for the initially ordered structures. The most important difference, however, is the observation that for the amorphous structure the temperature of the shocked state is always well defined.

The Hugoniot curve (Fig. 15) shows that at low piston velocities the velocity of the wave front at half height is almost constant. The distance between the bottom (amo\(_b\)) and the place where the wave reaches a constant value grows and the difference is most prominent around \( u_p/c_0 < 0.1 \). If the piston velocity is increased the ascent of the wave gets sharper and sharper until the difference between the velocities vanishes in the overdriven regime. The width of the transition region is of the order 5 to 10 atom distances \( a \).

In the RDF we find a rather sharp transition at the beginning of the overdriven regime at about \( u_p/c_0 < 0.4 \) (Fig. 16). At low piston velocities the first maximum of the RDF lies around 1.05\( a \), then it moves to 0.85\( a \) and broadens slightly. The most significant change occurs to the sharp sub-peak of the second maximum: It stays at its place, but broadens from a width of 0.4\( a \) to 0.5\( a \). The other sub-peak vanishes completely and the third maximum moves by 0.3\( a \) and doubles its width. At the highest piston velocities the RDF looks like one of an ordinary monoatomic liquid.

The ADF possesses two broad maxima at an angle of 60 degree and at 112 degree. In the shocked samples these maxima shift continuously to 57 and 110 degrees, respectively if the piston velocity is increased.

![FIG. 15: Hugoniot curve \( u_s \) vs. \( u_p \) for the amorphous structure. Plotted are the velocities at the bottom (amo\(_b\)), at half height (amo\(_h\)) and at the place where the hydrostatic pressure reaches a maximum (amo\(_g\)). In the overdriven region the distinction between these velocities vanishes, which means that we find sharp wave front.](image)
FIG. 16: RDF of the amorphous sample for different $u_p$. The arrows indicate how the RDF changes if the shock strength is increased from $u_p = 0.1c_a$ to $u_p = 0.8c_a$ ($c_a \approx 10\nu_0$).

FIG. 17: Relative frequency of the 1421 and 1422 common neighbor diagrams for some representative cases.

D. Common Neighbor Analysis

The common neighbor analysis has been carried out for all structures and orientations investigated in the preceding sections. Here we present only a representative selection. For the amorphous structure the fraction $n_{1421}/n_{1422}$ is always close to 0.5 (Fig. 17), which indicates complete disorder (Compare Honeycutt and Anderson22) and no crystallization. Therefore the distinction between fcc and hcp is difficult. We know however, that a bcc crystal shocked along the four-fold direction with $u_p = 0.24c_4$ results in nearly perfect hcp (Compare Fig. 10), and this structure has $n_{1421}/n_{1422} \approx 1$. Furthermore, perfect fcc should yield $n_{1421}/n_{1422} \rightarrow \infty$. Thus the higher values of $n_{1421}/n_{1422}$ clearly indicate fcc stacking. On the other hand it is obvious that disorder grows with increasing piston velocity.

From the diagram we read off three cases in addition the amorphous case: bcc shocked along the two-fold axis prefers fcc stacking at low piston velocities. The $\sigma$-phase shock in the m45-direction behaves similar. Bcc shocked along the three-fold direction behaves differently: it is hcp at low piston velocities and becomes preferably fcc stacked around $u_p/c_3 \approx 0.15$. Bcc shocked along the four-fold direction is always preferably hcp-stacked. The quasicrystal shocked along the 90-direction is similar. The other structures, the $\sigma$-phase shocked along the n45, m90 and 0-direction, the quasicrystal shocked along the 0-direction and the $\sigma$-phase along the n90-direction lie between bcc shocked along the three-fold and the four-fold direction, in the given ordering. The fluctuations of $n_{1421}/n_{1422}$ are large if the results for neighboring piston velocities are compared. The data should be regarded with some care especially for low piston velocities since the new phase forms rather slowly. For example the point at $u_p = 0.8c_4$, $n_{1421}/n_{1422} = 2.9$ may be too high. But if subsequent snapshots of the simulations are compared it is found that $n_{1421}/n_{1422}$ varies rather smoothly. Usually the results do not depend strongly on the size of the sample, but for the $\sigma$-phase shocked along the n45 and m45 it has been observed that special transition modes lead to a strong preference of hcp stacking.

IV. DISCUSSION

A. Comparison to Shock Wave Simulations of Iron

Kadai et al. have carried out molecular dynamics simulations of bcc iron single crystals.23,27 Instead of a simple pair potential they used EAM potentials especially adjusted to the properties of iron. Despite these differences their results and ours are in good qualitative agreement. There are several reasons for this observations: The phase diagram of iron28 and for the Dzugutov potential is similar, i.e., both possess at low temperatures a low pressure bcc and a high pressure close-packed phase. Furthermore, if the elastic constants are computed for the Dzugutov potential and compared with the relative values $c_{11}/c_{14}$ and $c_{21}/c_{44}$ for iron it is found that these values are closer in the diagrams (Fig. 2 of Every9) than to any other material.

Due to the similarity of the phase diagrams, the Hugo")n for iron (Kadai et al.25, Fig. 4) and bcc with Dzugutov potentials (Fig. 8) is qualitatively similar. The results for the four-fold direction are also in good agreement, however we did not observe the compressed bcc inclusions (Kadai et al.9, Fig. 1B). It is possible that they have been missed since their $u_p$-interval of occurrence is rather small.

Twinning is also prominent in our simulations (Fig. 11), and the growth of the crystalities with time (Kadai et al.25) has also been noticed. Another important coincidence15 are the solitary waves which occur for both interactions along the same three-fold direction. They will be discussed in detail in Paper II.

There are also some notable differences: The figures of
structures generated by shock waves along the two- and three-fold axis\textsuperscript{26} look similar at a first glance. Kadu et al. only remark that the grains in these situations are smaller than for the four-fold case. Furthermore a broad range of elastically compressed material is seen. The mechanism of phase transformation seems to be similar to the four-fold direction. But if we take our Figs. 12 and 13 into account we find a correlated transverse motion of lattice planes, i.e. a martensitic type of transformation\textsuperscript{31}. The \( \omega \)-phase has not been reported for EAM-iron. At last we want to remark that there is a difference in the final structures: The EAM potential clearly favors a hcp phase (Kadu et al.\textsuperscript{26}, Fig. 3), whereas we get a mixture of stackings of the close-packed layers. The reason for this difference is not obvious since the range of the EAM potential is similar to the range of the Dzugutov potential. We attribute the different behavior to the many-body part of EAM which is lacking for the pair potential. Therefore there is no difference in energy for ABA or ABC stacking for the Dzugutov potential whereas the EAM potential favors fec-ABC.

B. Conclusions

We have presented detailed studies of shock waves in several structures that are stabilized by the Dzugutov potential. There are at least three major results: The Dzugutov potential which has been designed for a completely different purpose is suitable to study qualitative features of bcc metals, such as iron. It may even be possible to get to a semi-quantitative or quantitative agreement if the Dzugutov potential is modified by fitting it directly to the iron properties. A second major result is the generation of special defects in the tcp phases which are equivalent to the phason flips in quasicrystals. This effect has been observed now on several occasions, here and in binary quasicrystals\textsuperscript{9}. Since the defects occur especially in the uniaxially compressed part of the sample it also represents evidence of the coupling between phasonic and phasonic degrees of freedom\textsuperscript{30} of a quasicrystal. In the end this means that although we have not (yet) found evidence for extended defects like phason walls generated by shock waves we have observed the creation of point defects and phason-type flips. Furthermore we have presented simulations of a Dzugutov glass and found that no crystallization occurs which tells us that the pre-existing bcc or tcp order helps the structures in the phase transition and shows that the transition is a correlated phenomenon.

Acknowledgments

I am especially indebted to H.-R. Trebin and Christoph Rudhart for many helpful discussions. The collaboration with Kai Kadu from Los Alamos National Lab and the hospitality there are also gratefully acknowledged. Franz Gähler supplied the data for the quasicrystal model.

15. J. Roth, "The \( \omega \)-Phase and Solitary Waves Induced by Shock Compression of BCC Crystals", submitted to Phys. Rev. B.
18. J. Roth, unpublished results.
31 In the interpretation of these results one has to be very careful if, for example, the coordination number is taken as an indication of the structure or defects since the material is compressed uniaxially and the ideal coordination numbers are no longer valid. If a radial criterion is used we find that a shift of the cutoff radius by less than a percent can change the picture completely since the atom shells of bcc and of the close-packed phase are rather broad and overlap partially which may mimic the presence of point defects (See Kadau et al.26, Fig. 2).